

Unraveling the transverse structure of nucleons with $p+\text{He-3}$ and $e+\text{He-3}$

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Workshop on opportunities for polarized He-3 in RHIC and EIC
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- Introduction
 - 3D structure of the hadron
 - spin as a tool to probe transverse motion
- Single spin asymmetries at RHIC
 - single inclusive hadron production: p-p, p-n, p-He3
 - Drell-Yan production: p-p, p-n, p-He3
- Sivers effect at EIC
 - e-p, e-n, e-He3
- Summary

Exploring the nucleon: of fundamental importance in science

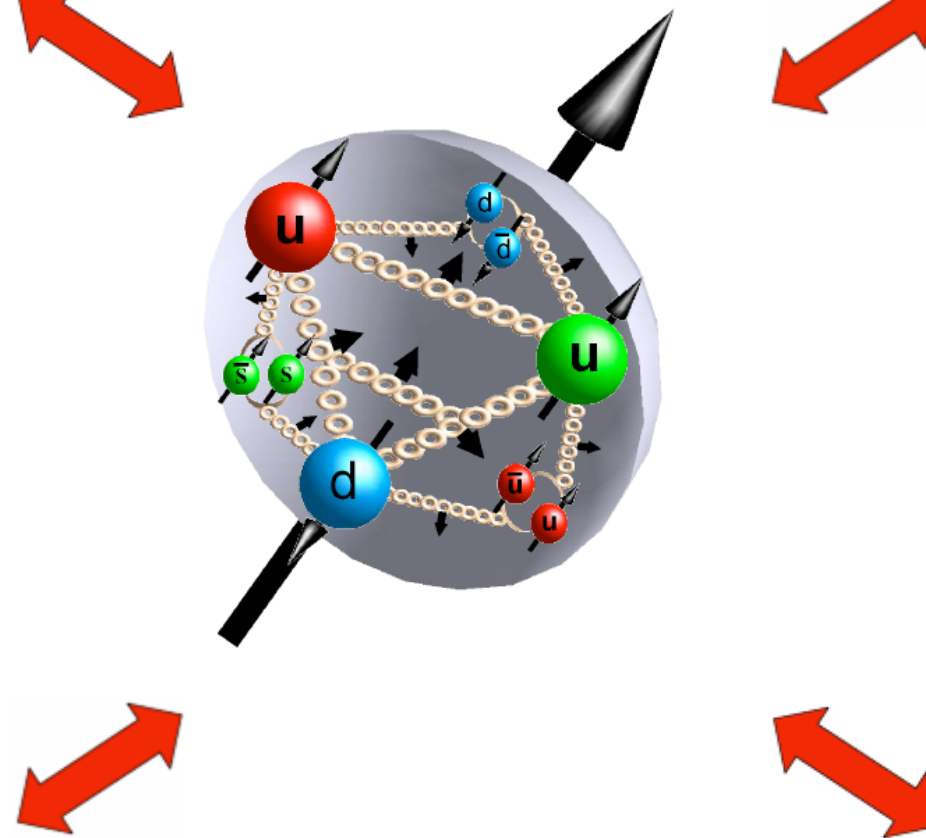
Know what we are made of:

**Most abundant particles
around us**

**Building blocks of all
elements**

Fundamental properties:

**Proton mass, spin,
magnetic moment,
understand them in terms
of the internal degrees of
freedom**



Tool for discovery:

Colliding high energy nucleons

New Physics beyond SM

LHC, Tevatron,

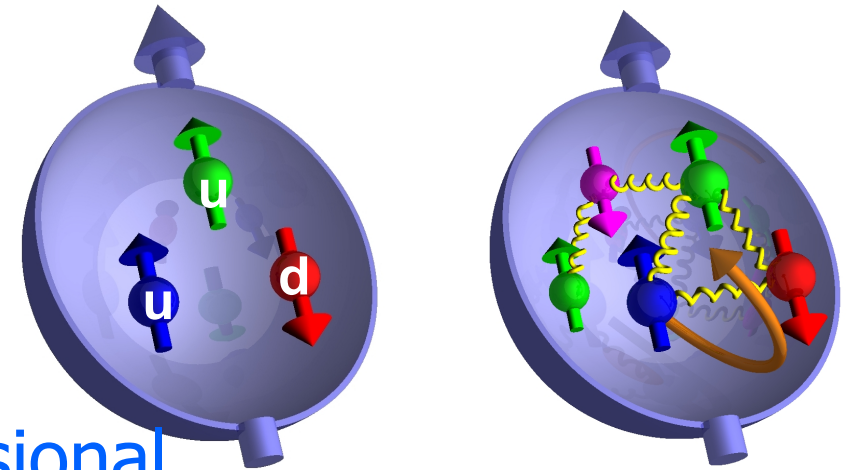
RHIC, HERA, ...

**Exploring QCD and
strong interaction:**

**Confinement,
Lattice QCD,
Asymptotic freedom,
perturbative QCD, ...**

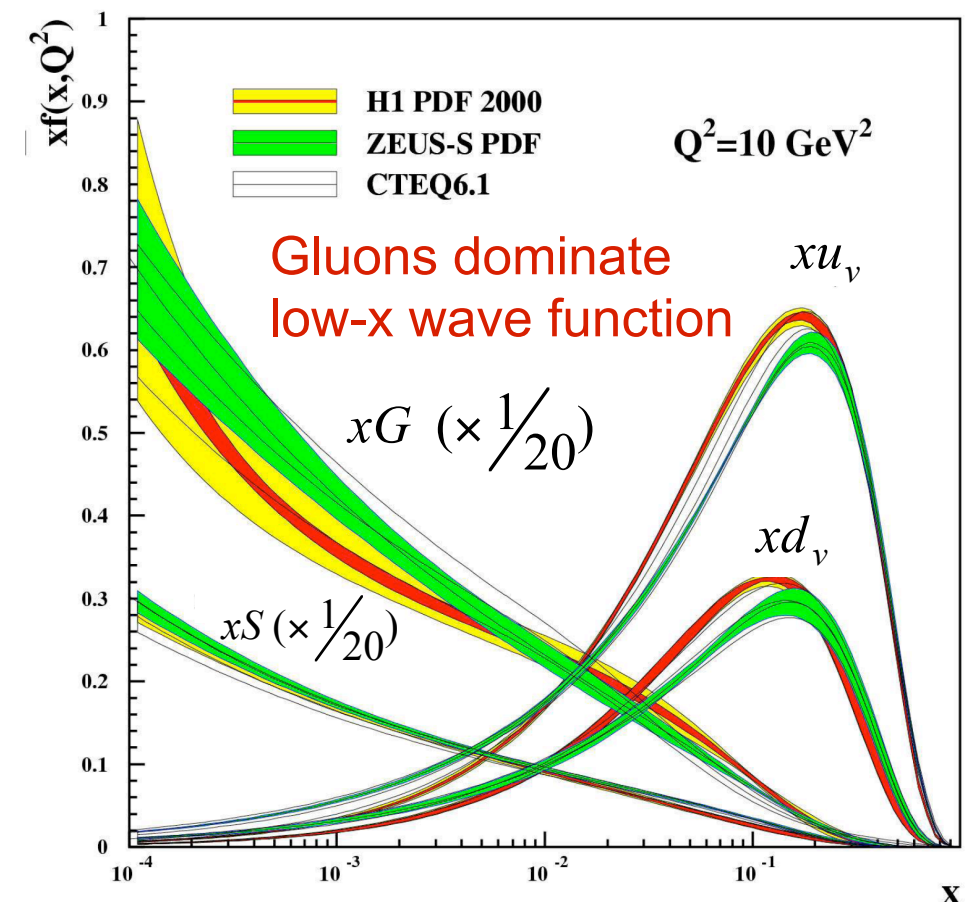
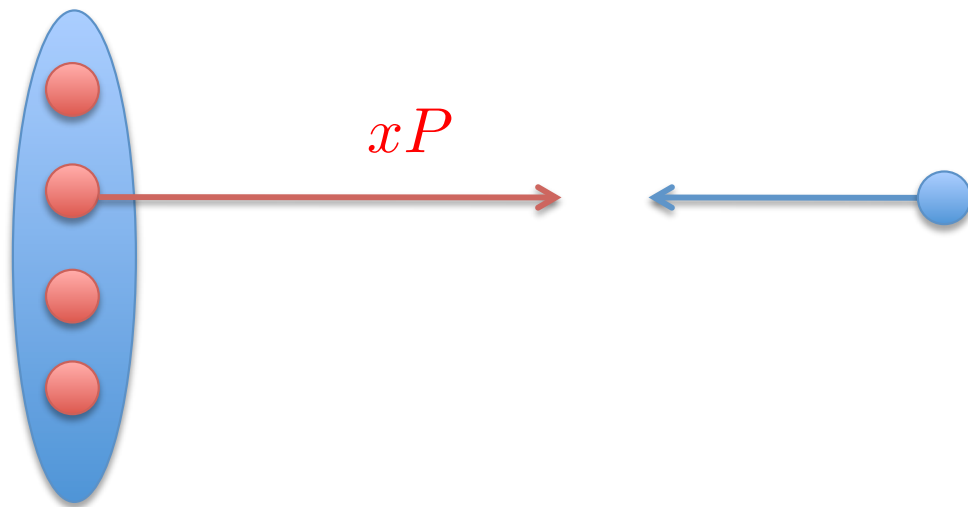
Hadron structure

- Proton is made of
 - 2 up quarks + 1 down quarks
 - + any number of quark-antiquark pairs
 - + any number of gluons
- So far the picture is more or less one-dimensional



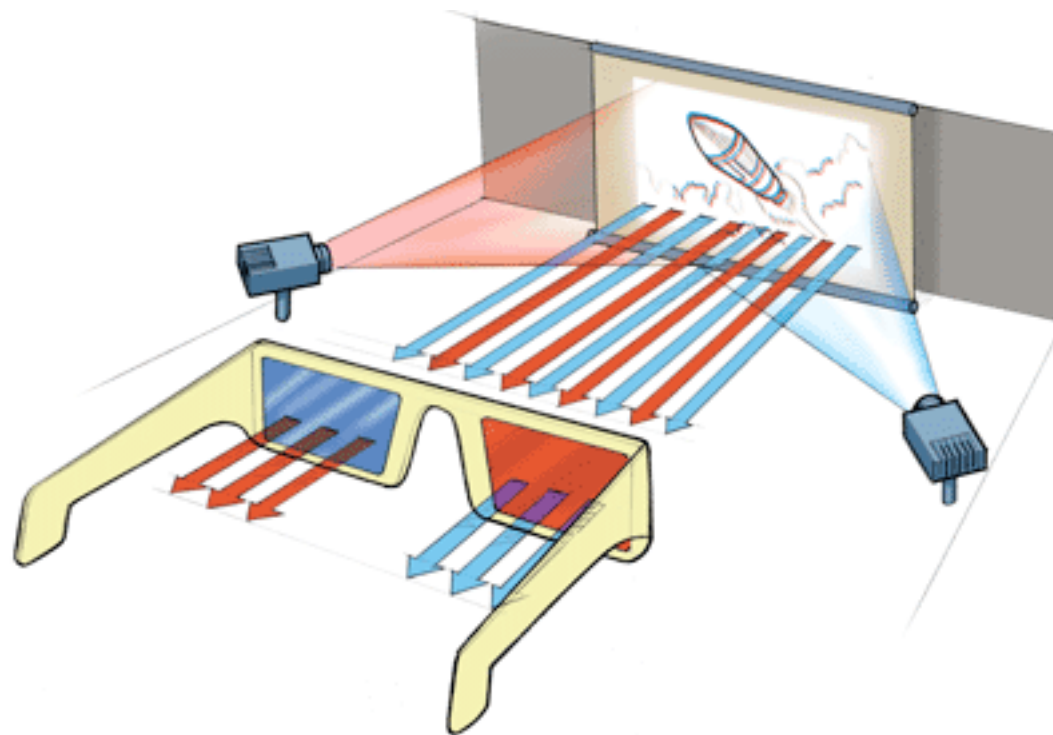
proton

electron



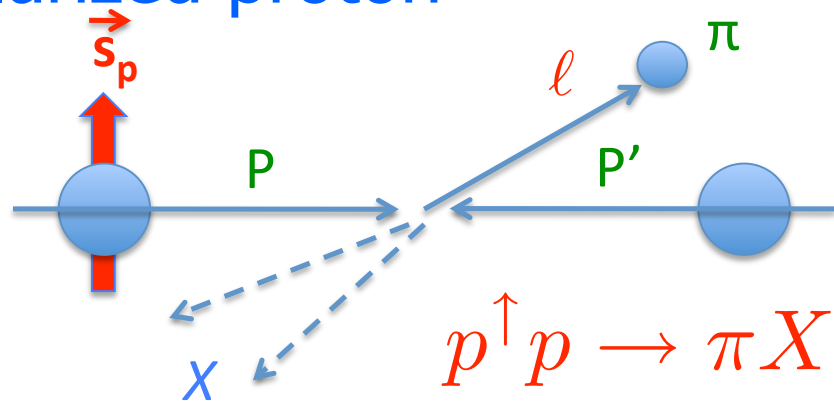
What about transverse motion?

- Uncertainty principle tells us that parton also carries transverse momentum $\langle k_{\perp} \rangle \sim \Lambda_{\text{QCD}}$
 - How do they move in the transverse plane?
 - Do they orbit, and carry orbital angular momentum?
 - moving from 1-dimension to 3-dimension

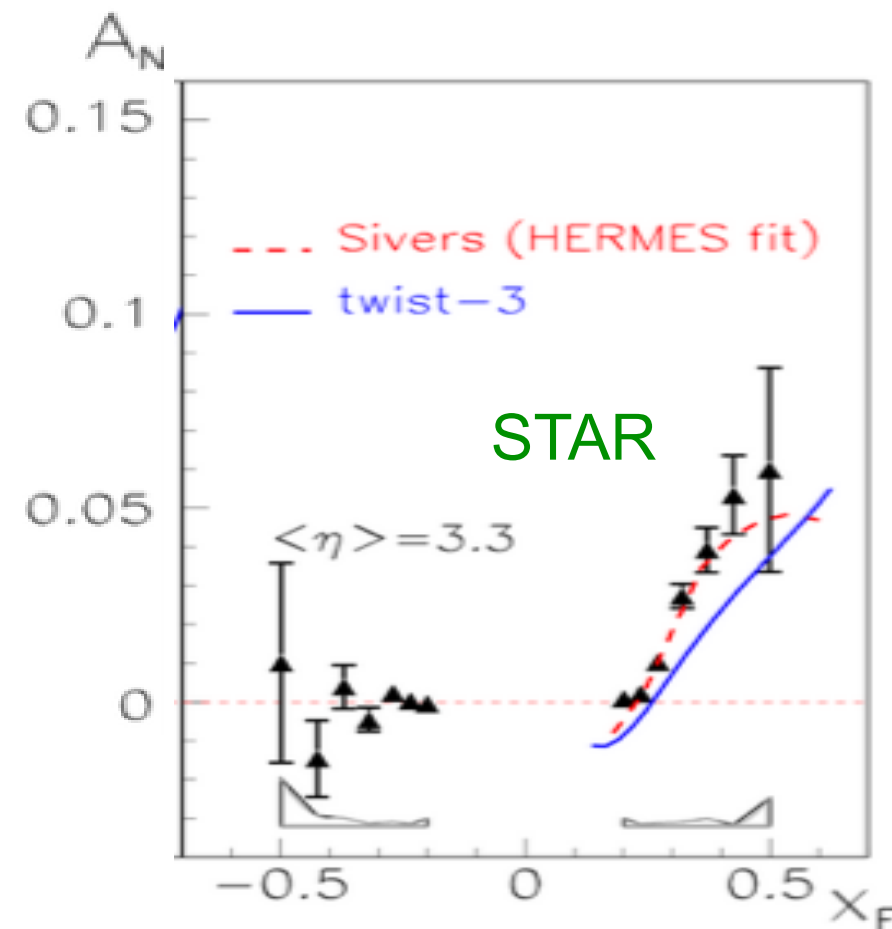
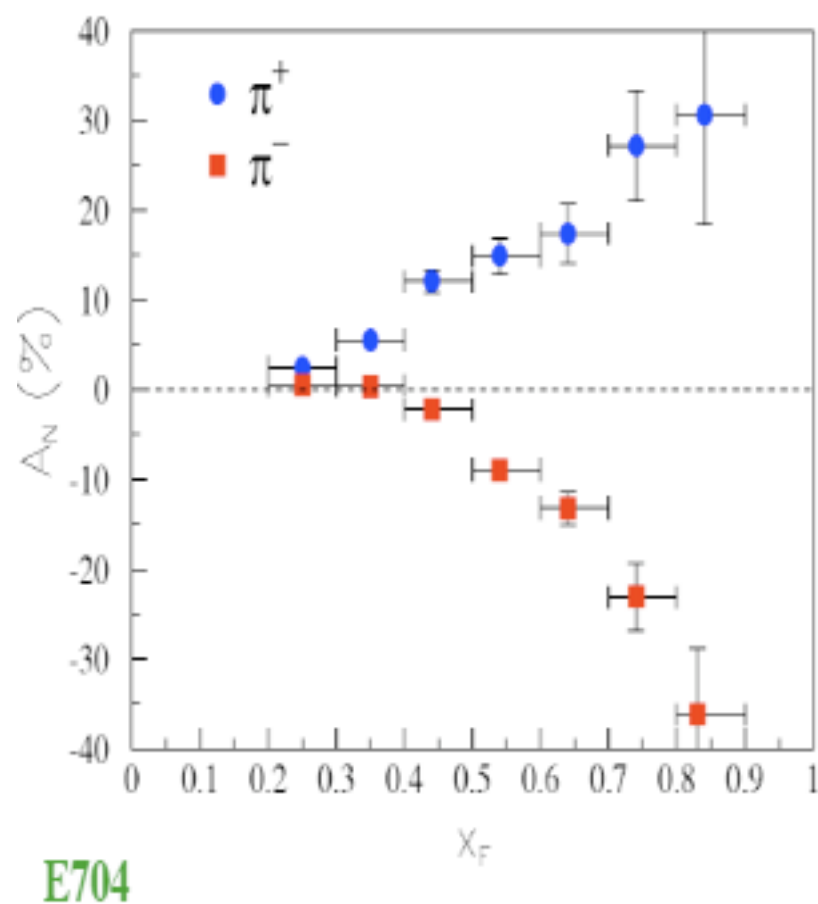


Single transverse spin asymmetry (SSA)

- Consider a transversely polarized proton scatters with another unpolarized proton



$$A_N \equiv \frac{\Delta\sigma(\ell, \vec{s})}{\sigma(\ell)} = \frac{\sigma(\ell, \vec{s}) - \sigma(\ell, -\vec{s})}{\sigma(\ell, \vec{s}) + \sigma(\ell, -\vec{s})}$$



PHENIX
HERMES
COMPASS
JLAB, too



SSA vanishes at leading twist in collinear factorization

- If partons are collinear (without transverse motion) Kane, Pumplin, Repko, 1978

$$A_N \sim \alpha_s \frac{m_q}{P_T} \rightarrow 0$$

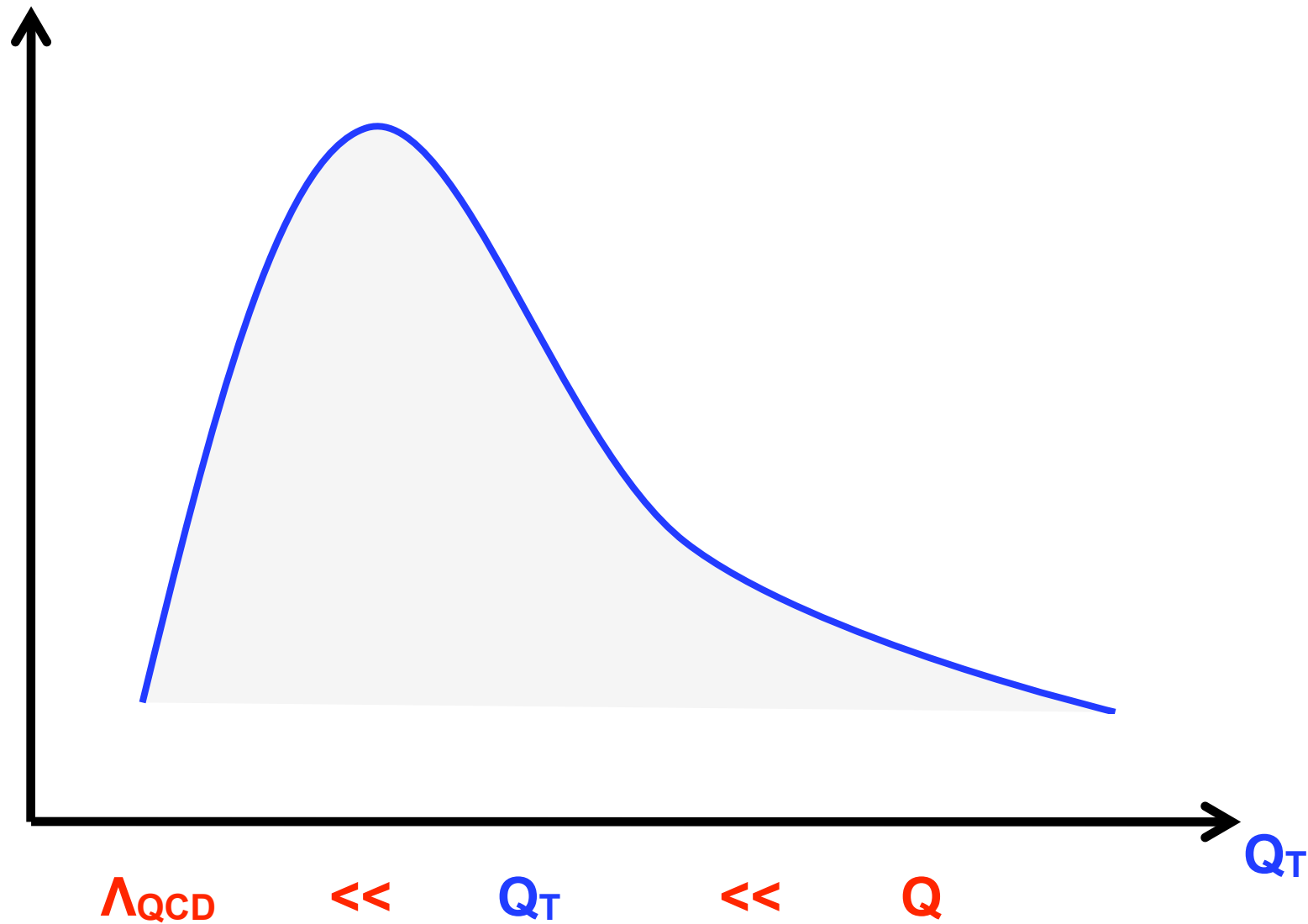
- $A_N \neq 0$: result of parton's transverse motion
- With transverse spin, one could then have many interesting correlation, which correlates spin and the transverse momentum of the parton. In other words, spin here is a useful tool to study parton's transverse motion.
 - In the incoming nucleon, there are 8 TMDs
 - For the outgoing produced pion, there are 2 TMDs



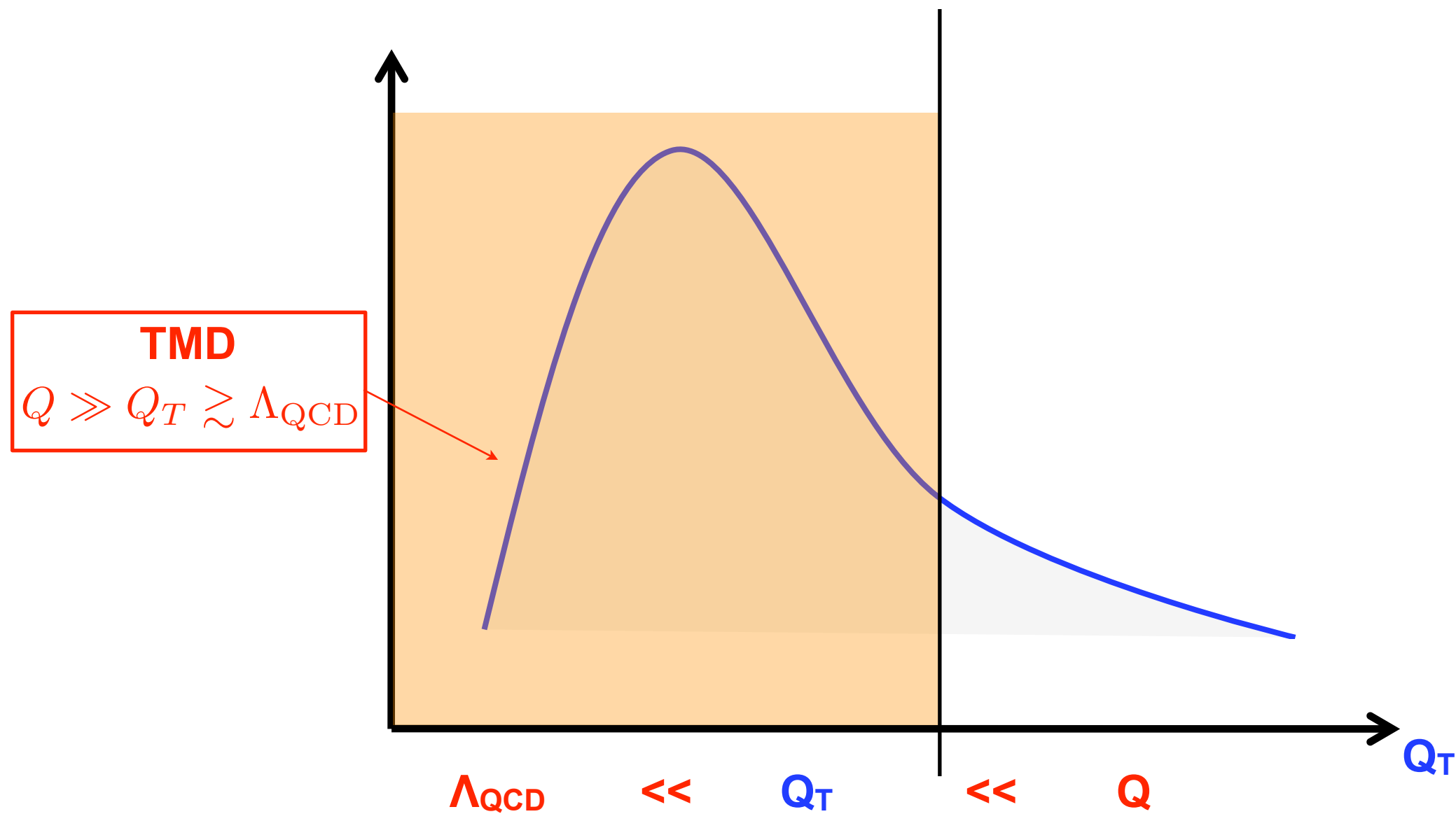
Two ways to contain transverse momentum

- One could immediately think of two ways to contain the parton transverse momentum
 - Generalize the collinear distribution $f(x)$ to $f(x, k_t)$
 - Taylor expansion: $f(x, k_t) = f(x) + k_t * f'(x) + \dots$, where $f'(x) = df(x, k_t)/dk_t$ at $k_t=0$. Then $\int d^2k_t k_t f'(x) =$ a higher-twist correlation
- The first approach is called TMD approach (transverse-momentum-dependent distribution)
- The second approach is called collinear twist-3 approach

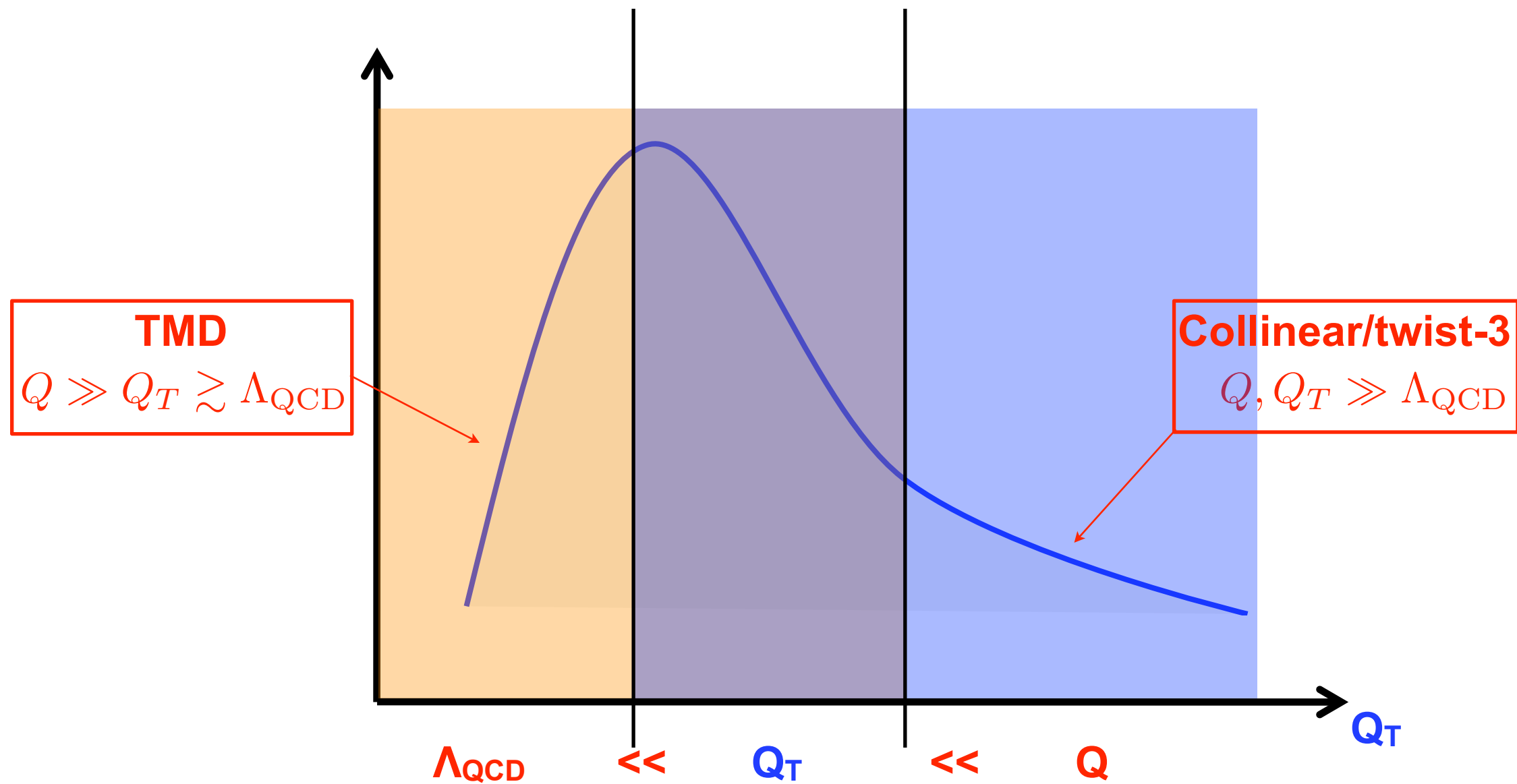
A unified picture for Drell-Yan (leading Q_T/Q)



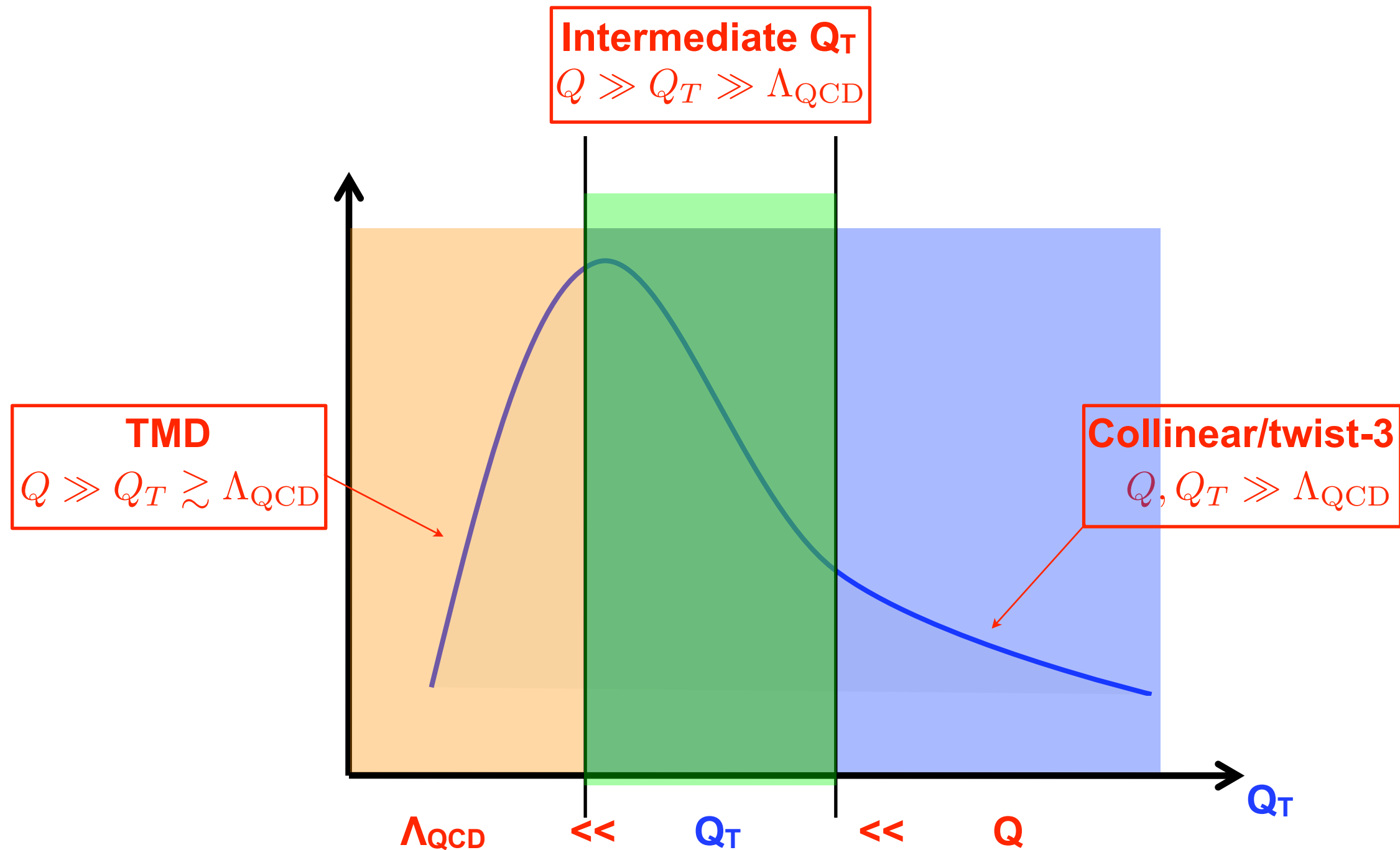
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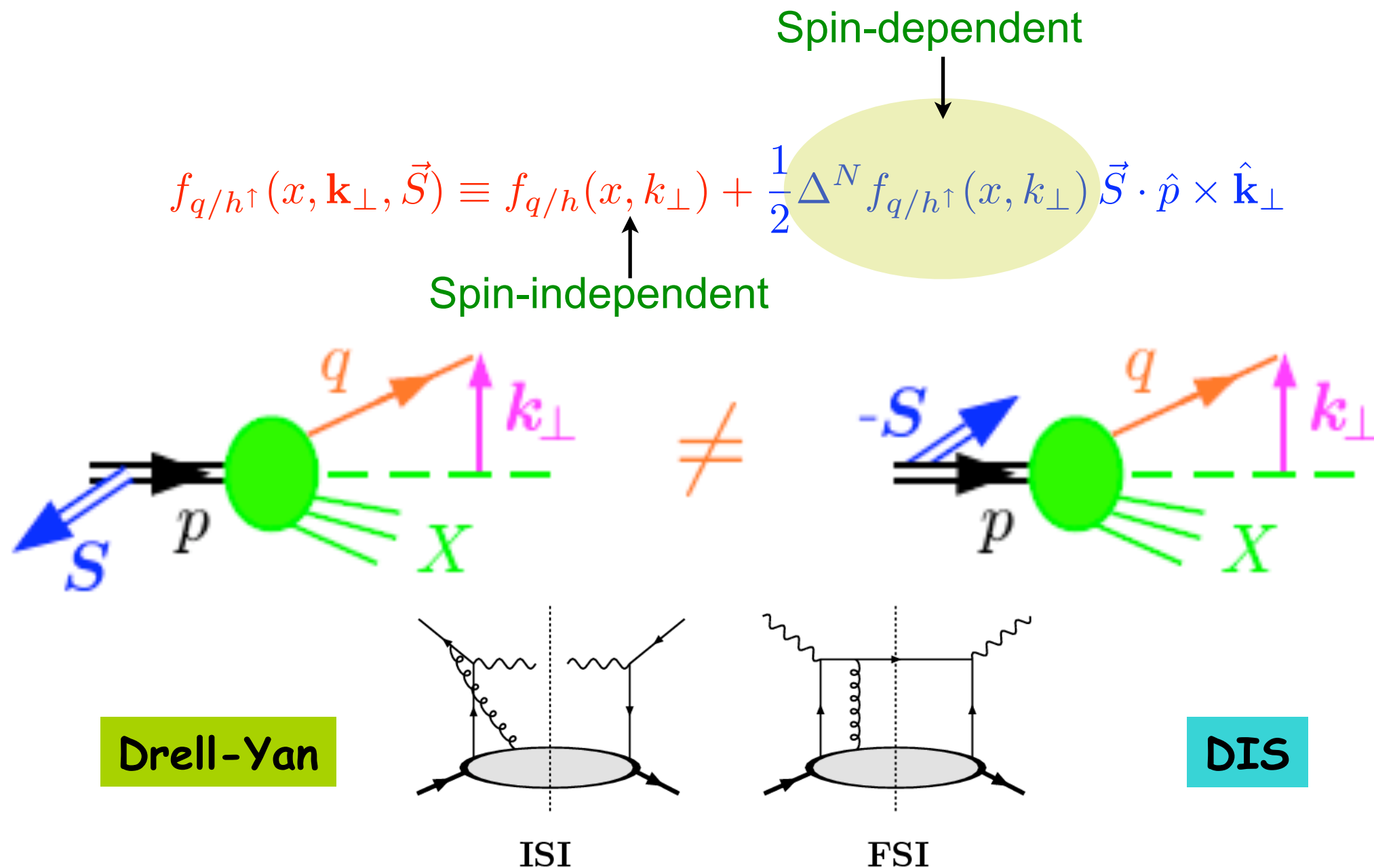


A unified picture for Drell-Yan (leading Q_T/Q)



Most discussed example

- Sivers function: an asymmetric parton distribution in a polarized hadron (k_t correlated with the spin of the hadron)

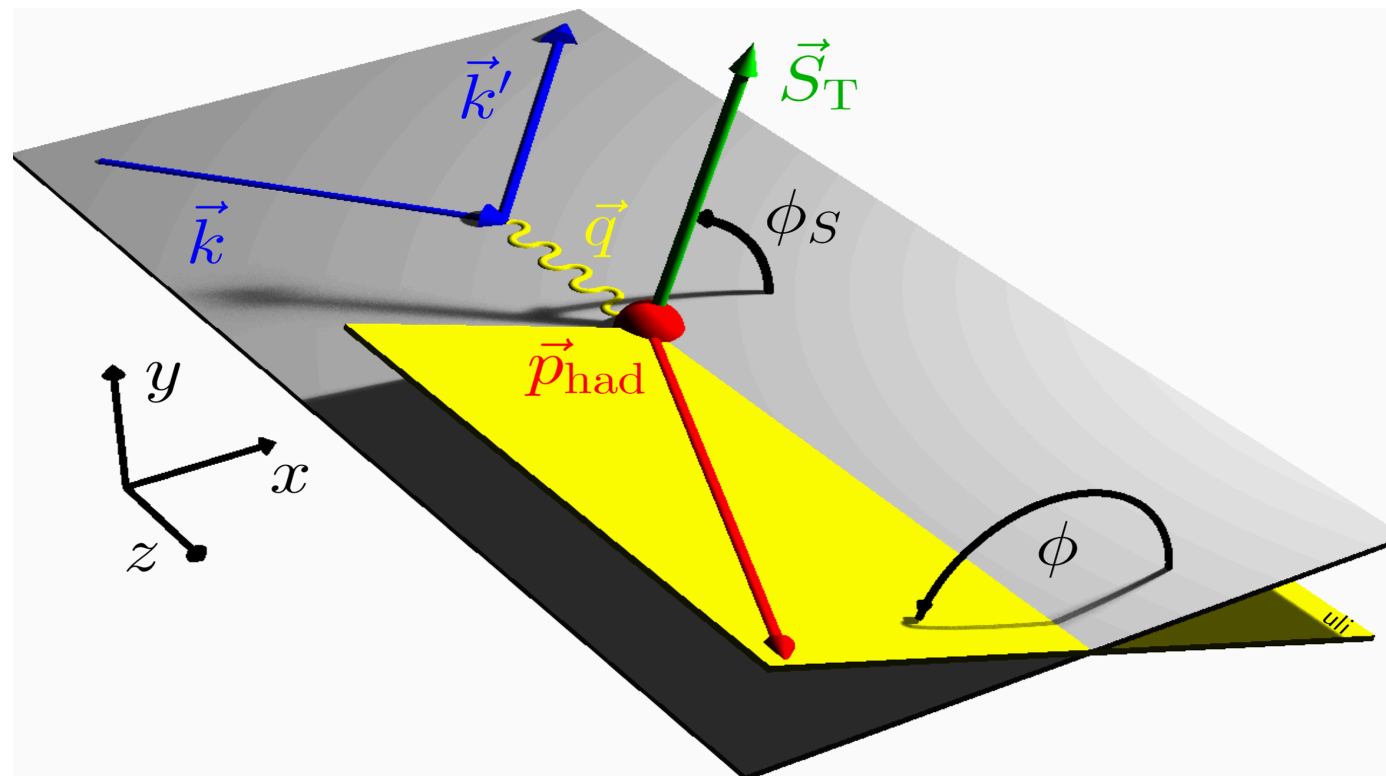


$$\text{Sivers}|_{\text{DY}} = -\text{Sivers}|_{\text{DIS}}$$

Current Sivers function from SIDIS

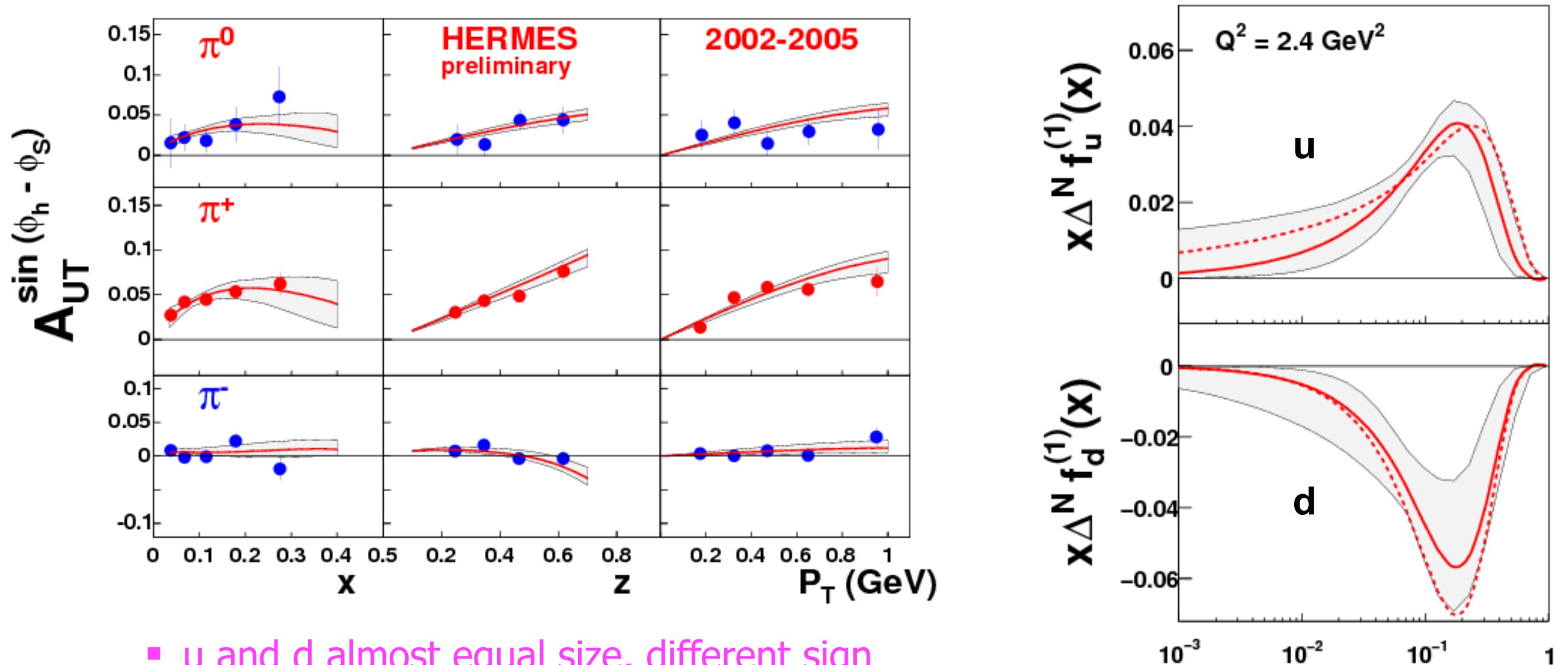
- Sivers and Collins can be separately extracted from SIDIS

$$\Delta\sigma \propto A_{\text{UT}}^{\text{Collins}} \sin(\phi + \phi_S) + A_{\text{UT}}^{\text{Sivers}} \sin(\phi - \phi_S)$$



Sivers function from SIDIS $\ell + p^\uparrow \rightarrow \ell' + \pi(p_T) + X : p_T \ll Q$

- Extract Sivers function from SIDIS (HERMES&COMPASS)



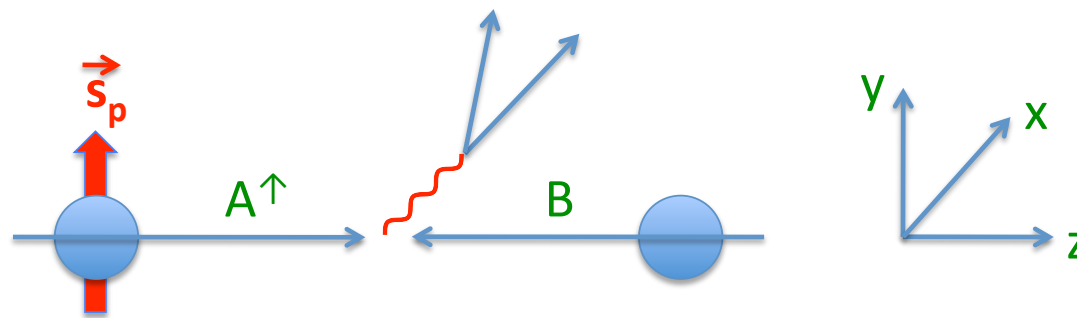
- u and d almost equal size, different sign
 - d -Sivers is slightly larger
- Still needs DY results to verify the sign change, thus fully understand the mechanism of the SSAs

Anselmino, et.al., 2009 \times

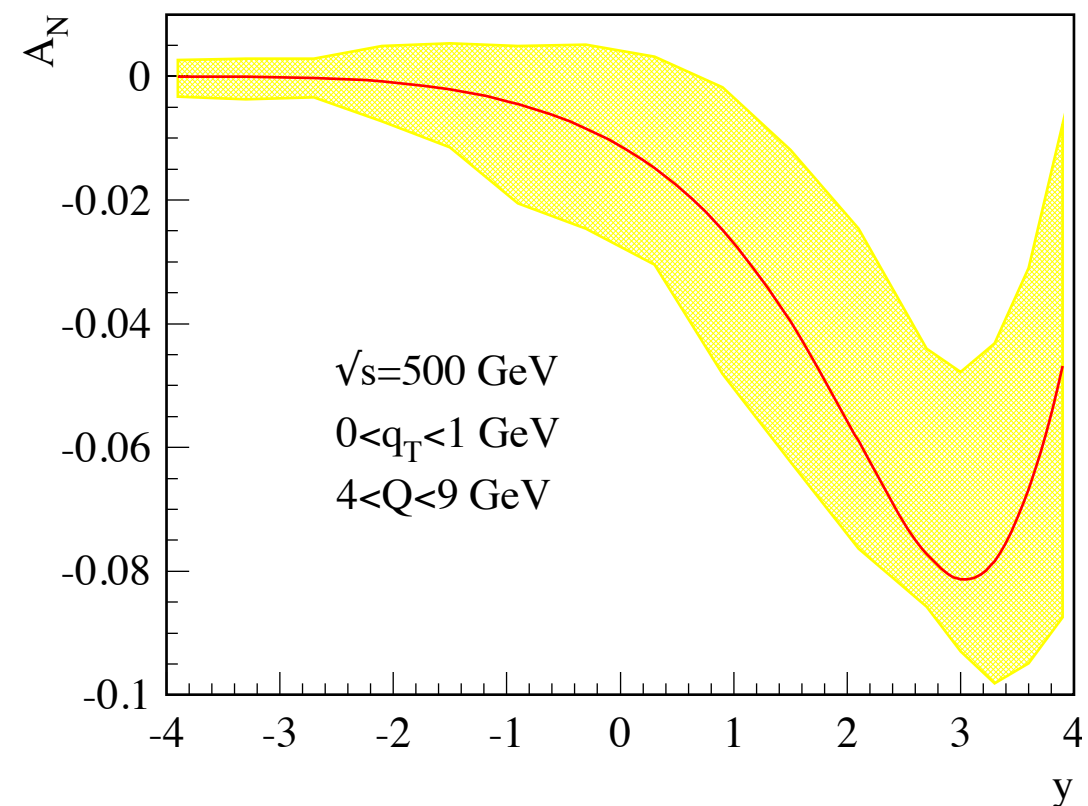
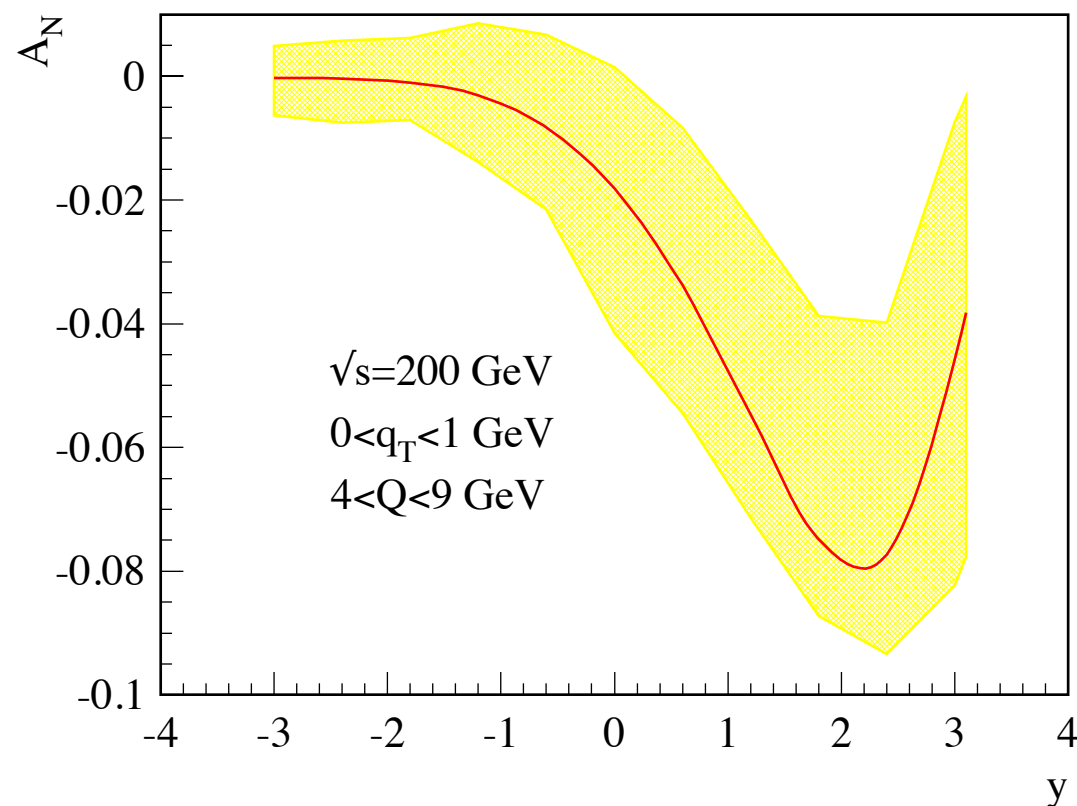
Predictions for Drell-Yan process at RHIC

- Reverse the sign of Sivers from SIDIS and make predictions for Drell-Yan production at RHIC

Kang-Qiu, PRD81, 2010



$$A_N \propto \frac{4}{9} \Delta^N u + \frac{1}{9} \Delta^N d < 0$$



polarized He-3

- Polarized He-3 is mainly a polarized neutron target:
 - polarized He-3: $0.865 \text{ n} + 2 \cdot (-0.027) \text{ p}$
 - unpolarized He-3: $\text{n} + 2 \cdot \text{p}$
- How the asymmetry will look like

$$A_p \sim \frac{\Delta f_p}{f_p} \qquad A_n \sim \frac{\Delta f_n}{f_n}$$

$$A_{3He} \sim \frac{0.865 \Delta f_n + 2 \cdot (-0.027) \Delta f_p}{f_n + 2f_p}$$

$$= 0.865 A_n \left(\frac{f_n}{f_n + 2f_p} \right) + 2 \cdot (-0.027) A_p \left(\frac{f_p}{f_n + 2f_p} \right)$$

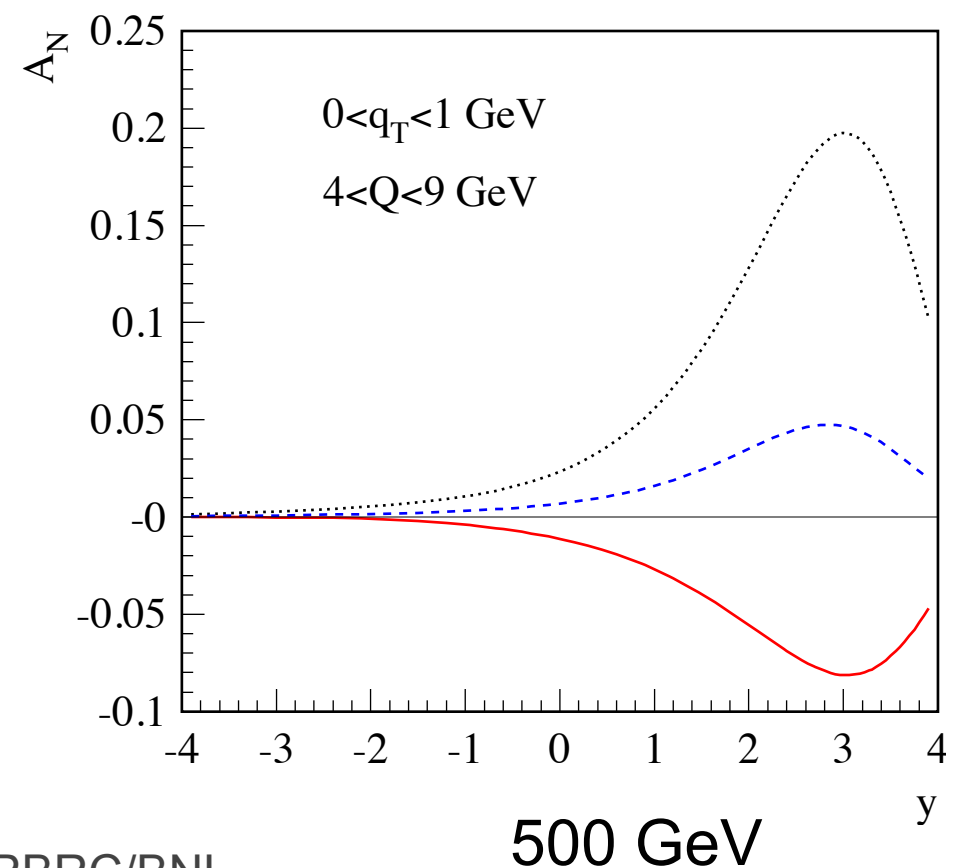
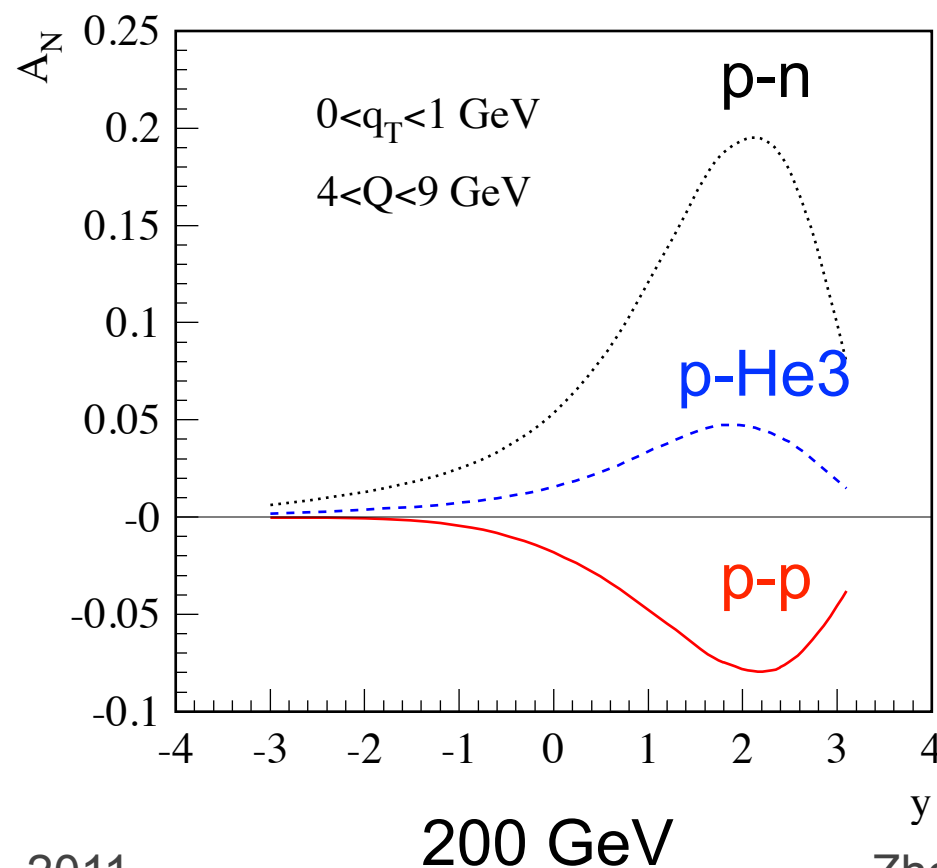
dilution factor

Drell-Yan production for p-p, p-n, p-He3

- Sign will be opposite to the proton case

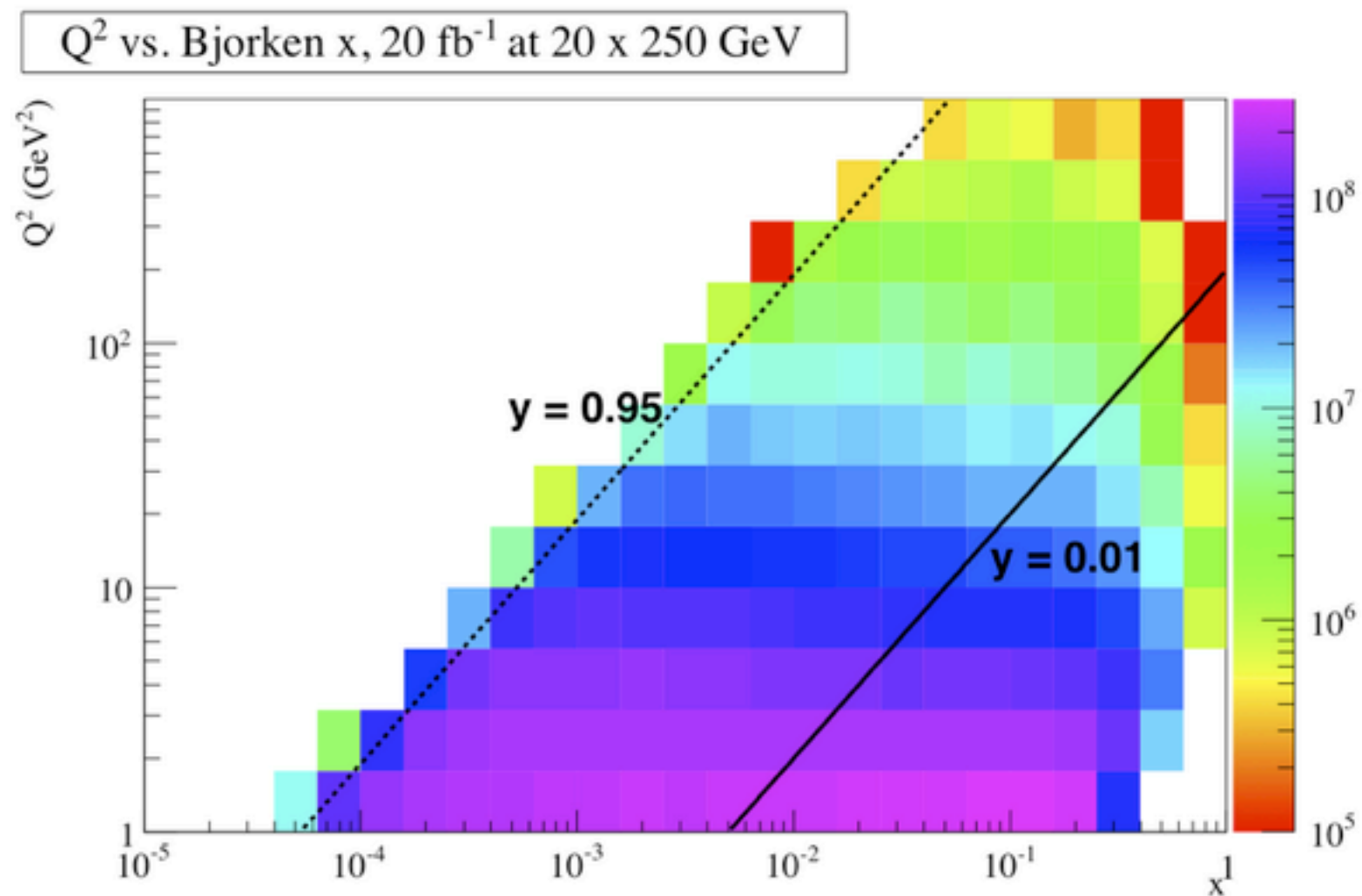
$$A_N = \frac{\sum_q e_q^2 \int \Delta^N f_{q/A^\uparrow}(x_1, \mathbf{k}_{\perp 1}) f_{\bar{q}/B}(x_2, k_{\perp 2})}{2 \sum_q e_q^2 \int f_{q/A}(x_1, k_{\perp 1}) f_{\bar{q}/B}(x_2, k_{\perp 2})} \propto \frac{4}{9} \Delta^N u_{\text{neutron}} + \frac{1}{9} \Delta^N d_{\text{neutron}} \\ = \frac{4}{9} \Delta^N d_{\text{proton}} + \frac{1}{9} \Delta^N u_{\text{proton}}$$

- d-Sivers is positive, $A_N > 0$
- d-Sivers is slightly larger, at the same time, it gets enhanced more by 4/9 compared with u-Sivers, thus the size of the asymmetry will be much bigger than the proton case



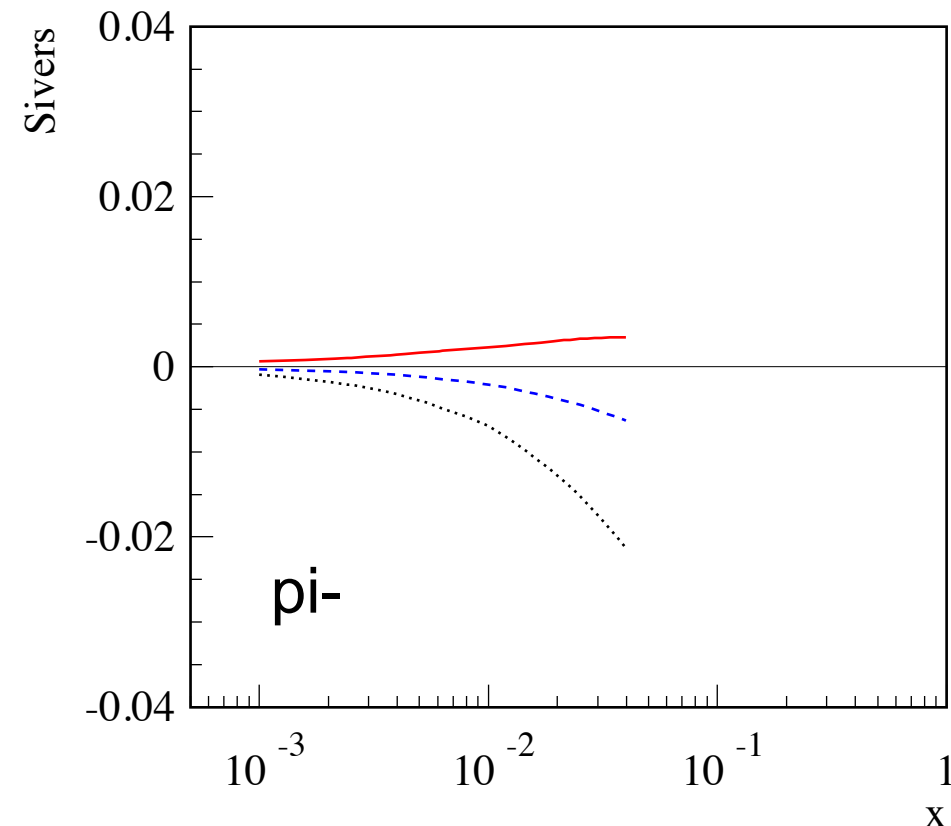
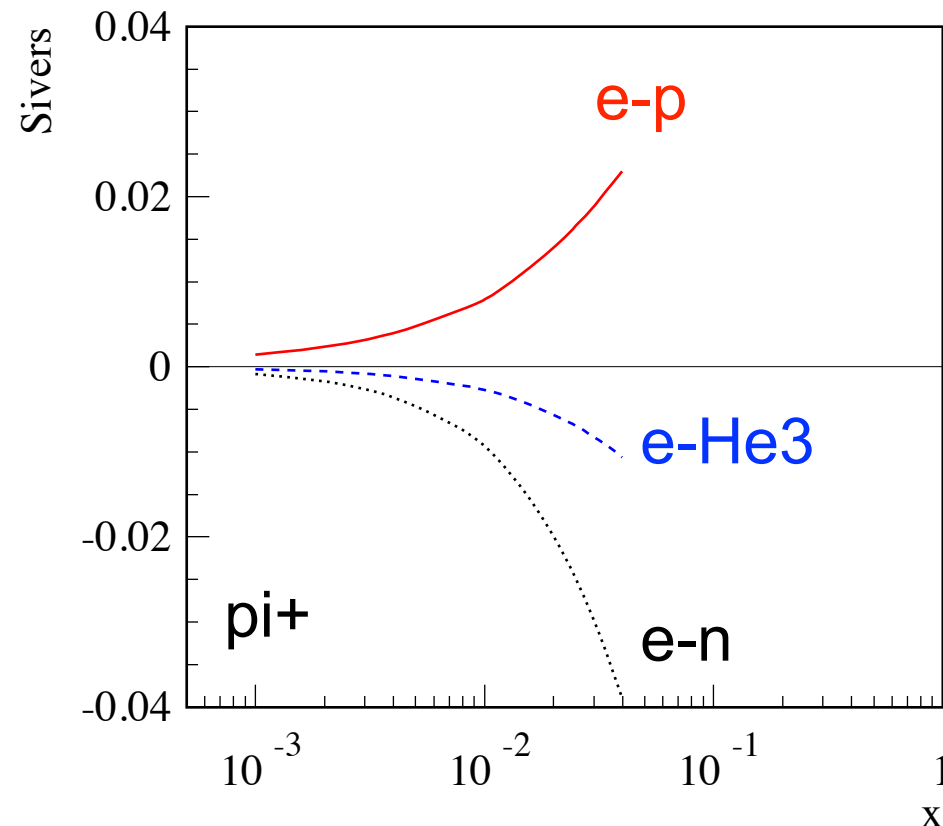
Future EIC

- Choose 20 GeV electron on 250 GeV proton
 - $Q^2 = 10 \text{ GeV}^2$
 - $0.01 < y < 0.95$



- Integrated for $0.4 < z < 0.6$, and $0 < p_t < 1$ GeV

$$A_N^{\sin(\phi_h - \phi_s)} \sim \frac{4}{9} \Delta^N u \cdot u \cdot D_u + \frac{1}{9} \Delta^N d \cdot d \cdot D_d$$



- Need a bit caution: Sivers function is only constrained at $x \sim [0.1, 0.3]$, EIC is mainly sensitive to low x region
- Some Collins estimate, see 1101.5196 (She and Ma)



Hadron production at RHIC

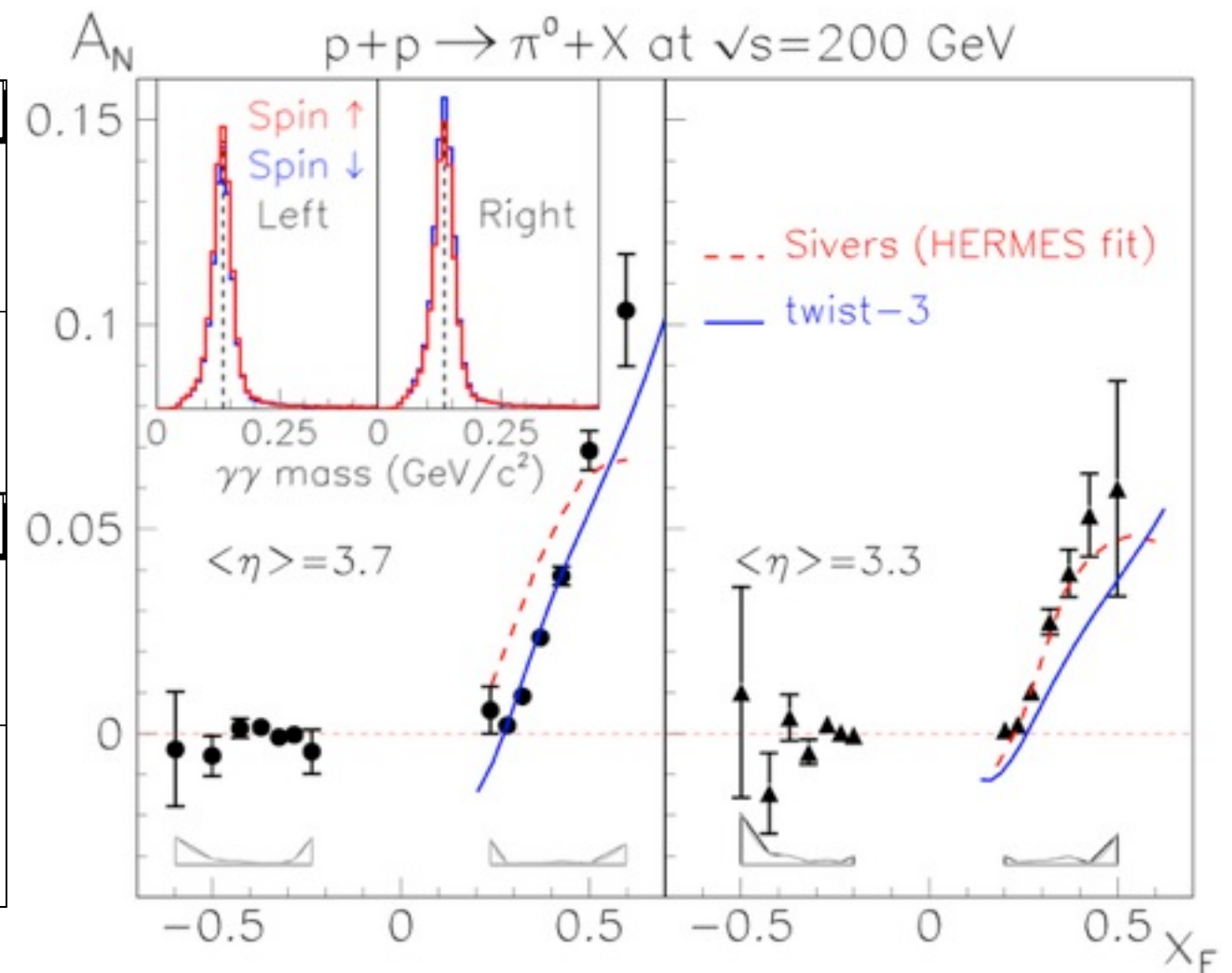
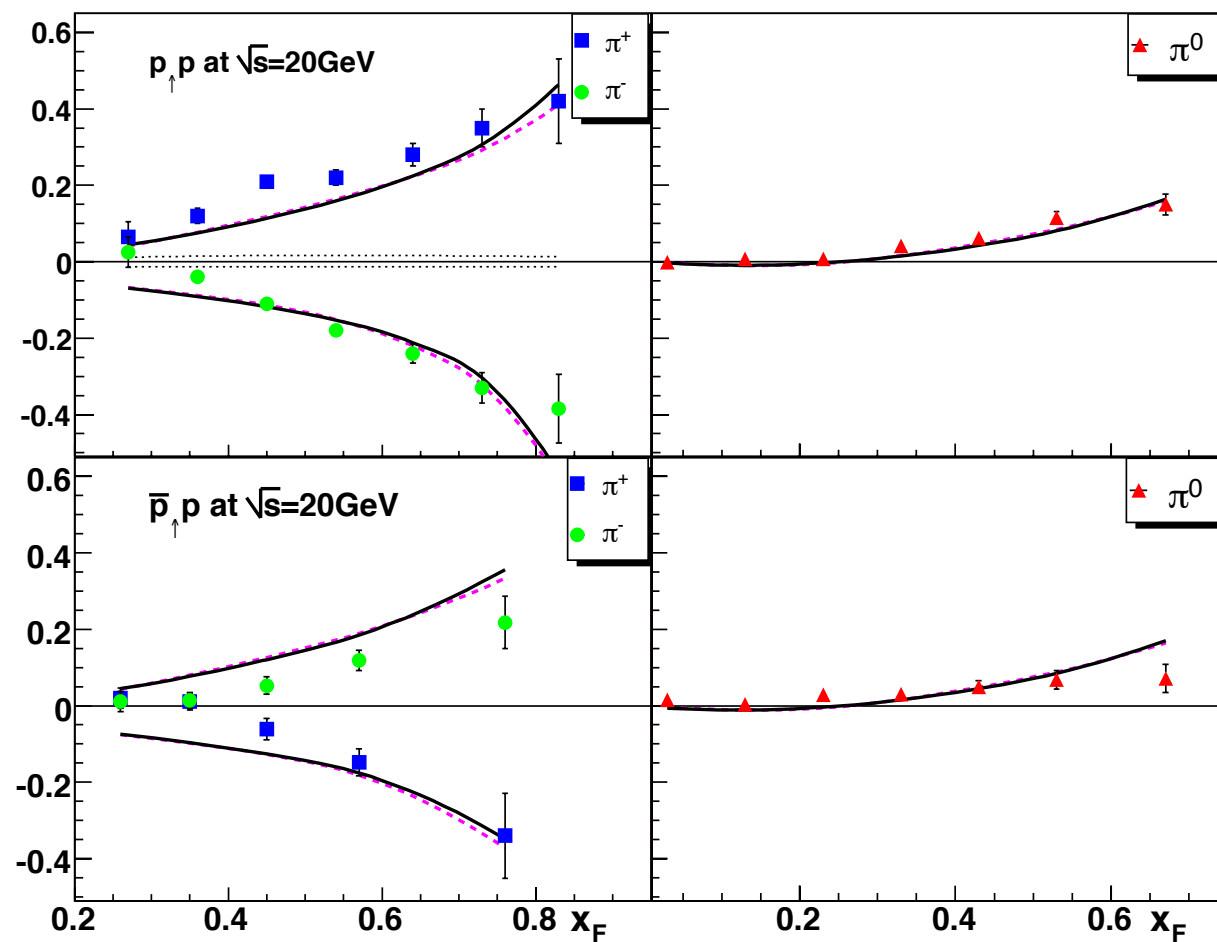
- Have the most data by far, but it is least understood
 - Sign mismatch Kang-Qiu-Vogelsang-Yuan, 2011
 - A complete picture consistent with all the available data (DIS, pp) is still not available Kang-Prokudin, still working ...
- With this in mind, we will still use the parametrization from year 2006. In the sense, it is at least consistent. Also the prediction should be reasonable Kouvaris-Qiu-Vogelsang-Yuan, 2006

Initial success of twist-3 approach

- Describe both fixed-target and RHIC well: a fit

$$T_{q,F}(x, x) = N_q x^{\alpha_q} (1 - x)^{\beta_q} \phi_q(x)$$

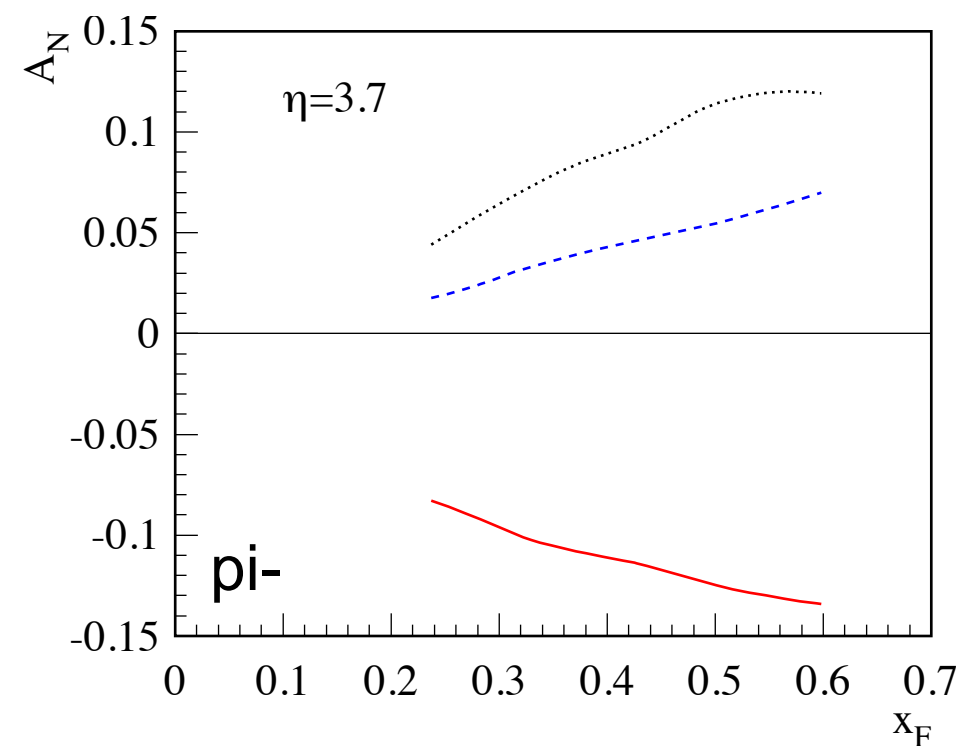
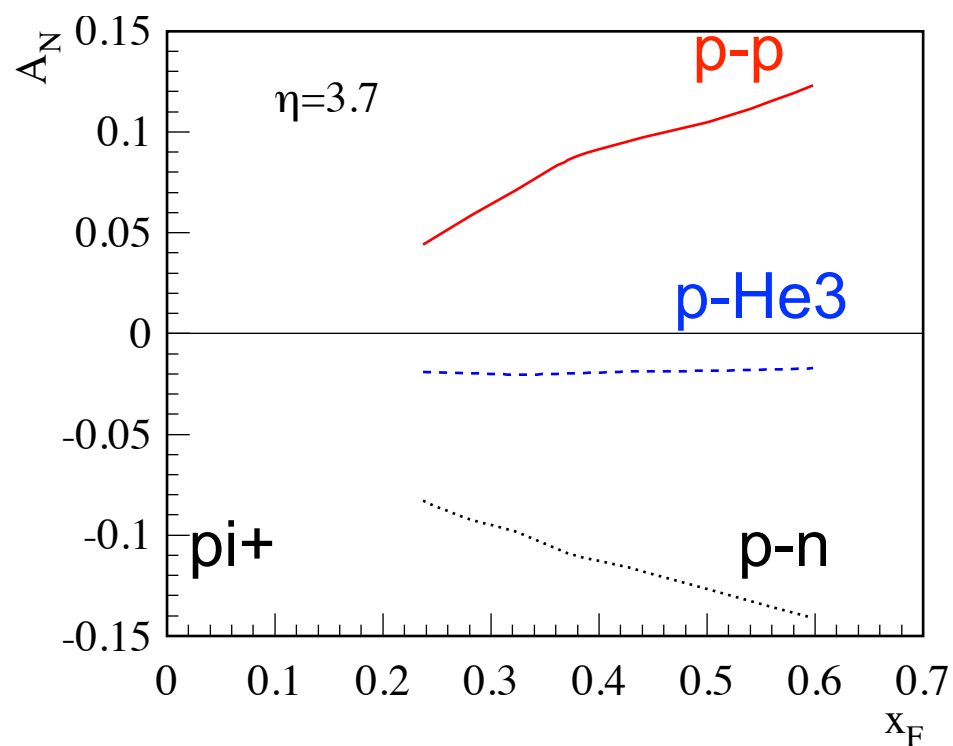
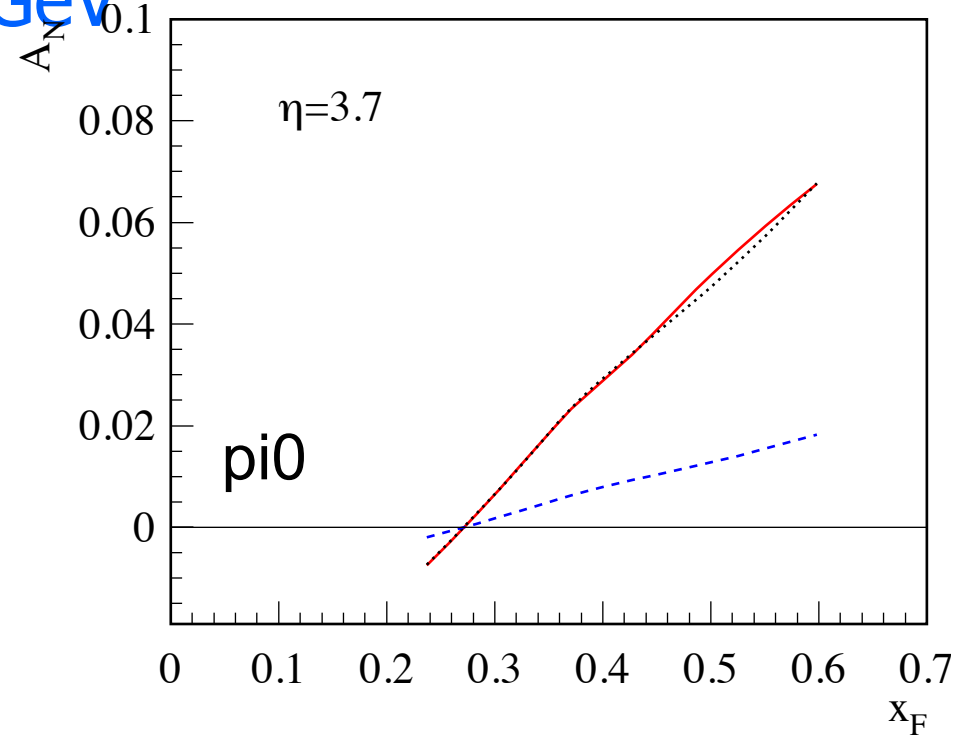
Kouvaris-Qiu-Vogelsang-Yuan, 2006



$$p^\uparrow p \rightarrow \pi + X$$

Single pion production

- CM energy 200 GeV





Summary

- Spin is a useful tool to probe hadron structure
- Spin-dependent distribution, Sivers function has opposite sign for u and d quark flavor
- Polarized He-3 could be used to confirm and verify this opposite sign
- If one could tag neutron, it typically leads to larger asymmetries
- Still need more data to establish the theory for the transverse spin phenomena: single inclusive jet, direct photon, Drell-Yan



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Thank you